

Warm Up: Vocabulary

Define consecutive

Define integer

9/8 Equations Involving Consecutive Integers

1) Find two consecutive integers whose sum is 211.

1st integer: x
2nd integer: $x+1$

$$x + x + 1 = 211$$

$$\begin{array}{r} 2x + 1 = 211 \\ -1 \quad -1 \\ \hline \end{array}$$

$$\frac{2x}{2} = \frac{210}{2}$$

$$x = 105$$

The two consecutive integers are 105 + 106.

3) Find two consecutive **odd** integers whose sum is 68.

1st odd integer: x
2nd odd integer: $x+2$

$$x + x + 2 = 68$$

$$\begin{array}{r} 2x + 2 = 68 \\ -2 \quad -2 \\ \hline \end{array}$$

$$\frac{2x}{2} = \frac{66}{2}$$

$$x = 33$$

The two ^{cons.} odd integers are 33 + 35.

5) Find five consecutive integers whose sum is 395.

$$\underbrace{x} + \underbrace{x+1} + \underbrace{x+2} + \underbrace{x+3} + \underbrace{x+4} = 395$$

$$5x + 1 + 2 + 3 + 4 = 395$$

$$5x + 10 = 395$$

- 1st = 77
- 2nd = 78
- 3rd = 79
- 4th = 80
- 5th = 81

$$\begin{array}{r} -10 \quad -10 \\ 5x = 385 \\ \hline 5 \quad 5 \end{array}$$

Part 2

7) Find two consecutive **odd** integers whose sum is -88.

1st odd integer: x
 2nd odd integer: $x+2$

$$x + x + 2 = -88$$

$$\begin{array}{r} 2x + 2 = -88 \\ -2 \quad -2 \\ \hline \end{array}$$

$$\begin{array}{r} 2x = -90 \\ \hline 2 \quad 2 \end{array}$$

$$x = -45$$

The two consecutive odd integers are -45 + -43.

- 9) Find two consecutive **even** integers such that the sum of the larger and twice the smaller is 62.

1st even integer: x
 2nd even integer: $x+2$

larger $x+2$ + *twice the smaller* $2x = 62$

$$\begin{array}{r} 3x + 2 = 62 \\ -2 \quad -2 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \cdot x = 60 \\ \hline 3 \quad 3 \end{array}$$

$$x = 20$$

20, 22

- 11) Find three consecutive **odd** integers such that the sum of the smallest and 4 times the largest is 61.

1st odd int x
 2nd odd int $x+2$
 3rd odd int $x+4$

$$x + 4(x+4) = 61$$

$$\begin{array}{r} x + 4x + 16 = 61 \\ \hline 5x + 16 = 61 \end{array}$$

1st = 9
 2nd = 11
 3rd = 13

$$\begin{array}{r} 5x + 16 = 61 \\ -16 \quad -16 \\ \hline 5x = 45 \end{array}$$

$$\begin{array}{r} 5x = 45 \\ \hline 5 \quad 5 \\ \hline x = 9 \end{array}$$