

4/19 Add, Subtract, and Multiply Radical Expressions

Add/Subtract Radicals: Think - Combine Like Terms
the "terms" must have the exact same radicand. (what's in the square root.)

* $2\sqrt{3} + 8\sqrt{3} = 10\sqrt{3}$ similar to $2x + 8x = 10x$

* $4\sqrt{10} + \sqrt{13} - 9\sqrt{10}$
 $-5\sqrt{10} + \sqrt{13}$

* $7\sqrt{14} + \sqrt{21} - 4\sqrt{14}$
 $3\sqrt{14} + \sqrt{21}$

* $2\sqrt{3} + \sqrt{7} + \sqrt{3} + 6\sqrt{7}$ $\sqrt{3}$ and $\sqrt{7}$
 $3\sqrt{3} + 7\sqrt{7}$ have a "coefficient"
of 1.

* $2\sqrt{11} + \sqrt{99}$ → $\sqrt{99}$
 $2\sqrt{11} + 3\sqrt{11}$ $\sqrt{9}\sqrt{11}$
 $5\sqrt{11}$ $3\sqrt{11}$

* $5\sqrt{7} + \sqrt{28}$ → $\sqrt{28}$
 $5\sqrt{7} + 2\sqrt{7}$ $\sqrt{4}\sqrt{7}$
 $7\sqrt{7}$ $2\sqrt{7}$

$$\begin{aligned}
 * \quad & \sqrt{45} + 3\sqrt{20} \\
 & \sqrt{9\sqrt{5}} + 3\sqrt{4\sqrt{5}} \\
 & 3\sqrt{5} + 3 \cdot 2\sqrt{5} \\
 & 3\sqrt{5} + 6\sqrt{5} \\
 & \boxed{9\sqrt{5}}
 \end{aligned}$$

Multiply Radical Expressions

Distributive Property.

$$\begin{aligned}
 * \quad & \xrightarrow{\text{Dist. Prop}} \sqrt{3}(2 + \sqrt{12}) \\
 & 2\sqrt{3} + \sqrt{36} \\
 & \boxed{2\sqrt{3} + 6}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{3}(2 \cdot \sqrt{12}) \\
 & \sqrt{3} * 2 * \sqrt{12} \quad \text{Multiplication only.}
 \end{aligned}$$

$$\begin{aligned}
 * \quad & \sqrt{3}(12 - \sqrt{15}) \\
 & 12\sqrt{3} - \sqrt{45} \\
 & \quad \quad \quad \sqrt{9\sqrt{5}} \\
 & \boxed{12\sqrt{3} - 3\sqrt{5}}
 \end{aligned}$$

$$\begin{aligned}
 * \quad & 3\sqrt{6}(4\sqrt{6} - \sqrt{600}) \quad \rightarrow \quad \sqrt{600} \\
 & 3\sqrt{6}(4\sqrt{6} - 10\sqrt{6}) \quad \quad \quad \sqrt{100}\sqrt{6} \\
 & 3\sqrt{6}(-6\sqrt{6}) \quad \quad \quad 10\sqrt{6} \\
 (3x-6) \quad & -18\sqrt{36} \quad \quad \quad \text{Multiply} \\
 & -18 \cdot 6 \\
 & \boxed{-108}
 \end{aligned}$$

$$* (6 - \sqrt{7})^2$$

$$= (6 - \sqrt{7})(6 - \sqrt{7})$$

$$= 36 - 6\sqrt{7} - 6\sqrt{7} + \sqrt{49}$$

$$= 36 - 12\sqrt{7} + 7$$

either $\left\{ \begin{array}{l} 43 - 12\sqrt{7} \\ -12\sqrt{7} + 43 \end{array} \right.$

	6	$-\sqrt{7}$	
6	36	$-6\sqrt{7}$	$-12\sqrt{7}$
$-\sqrt{7}$	$-6\sqrt{7}$	$\sqrt{49} = 7$	$36 + 7 = 43$

$$43 - 12\sqrt{7}$$

OR

$$-12\sqrt{7} + 43$$

$$* (\sqrt{2} + \sqrt{5})(\sqrt{2} - 3\sqrt{5})$$

$$= \sqrt{4} - 3\sqrt{10} + \sqrt{10} - 3\sqrt{25}$$

$$= 2 - 2\sqrt{10} - 3 \cdot 5$$

$$= 2 - 2\sqrt{10} - 15$$

$$\boxed{-13 - 2\sqrt{10}}$$

OR

$$\boxed{-2\sqrt{10} - 13}$$